

Modern Physics-III - Stability of Nuclei

Q.1. Find mass of ${}_{7}^{14}\text{N}$
 $p \rightarrow 7$
 $n \rightarrow 7$
 $e^- \rightarrow 7$

$$\Delta m = \begin{cases} m({}_{7}^{14}\text{N})_{\text{expected}} = (7 \times 1.00783 + 7 \times 1.00867 + 7 \times 0.0005486) \text{ u} \\ = 14.119368 \text{ u} \\ m({}_{7}^{14}\text{N})_{\text{obs}} = 14.00307 \text{ u} \end{cases}$$

$\Delta m = 0.116298 \text{ u}$
 $\equiv 108.33 \text{ MeV}/c^2$

$\Delta E = 108.33 \text{ MeV}$

$${}_{26}^{56}\text{Fe} \rightarrow \begin{cases} m({}_{26}^{56}\text{Fe})_{\text{expected}} = 26 \times (1.00783) \\ \quad + 30 \times (1.00867) \\ \quad + 26 \times (0.0005486) \\ = 56.47887 \text{ u} \\ m({}_{26}^{56}\text{Fe})_{\text{obs}} = 55.9349 \text{ u} \\ \Delta m = 0.54397 \text{ u} \equiv 506.70 \text{ MeV}/c^2 \end{cases}$$

$$\begin{aligned} m({}_{1}^1\text{H}) &= 1.00783 \text{ u} \\ m({}_{1}^0\text{n}) &= 1.00867 \text{ u} \\ m({}_{-1}^0\text{e}) &= 0.0005486 \text{ u} \\ \boxed{1 \text{ u} &\equiv 931.5 \text{ MeV}/c^2} \end{aligned}$$

Q.2 α particle, ${}_{2}^4\text{He}$
 $p \rightarrow 2$
 $n \rightarrow 2$
 $e^- \rightarrow 2$

$$\begin{aligned} m({}_{2}^4\text{He})_{\text{expected}} &= 2 \times 1.00783 + 2 \times 1.00867 \\ &\quad + 2 \times 0.0005486 \\ &= 4.17503 \text{ u} \end{aligned}$$

$$m({}_{2}^4\text{He})_{\text{obs}} = 4.00260 \text{ u}$$

$$\begin{aligned} \Delta m &= 0.17243 \text{ u} \\ &= 160.62 \text{ MeV}/c^2 \end{aligned}$$

$$\boxed{\Delta E = \Delta m c^2 = 160.62 \text{ MeV}}$$

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$$m({}_1^1\text{H}) = 1.007834$$

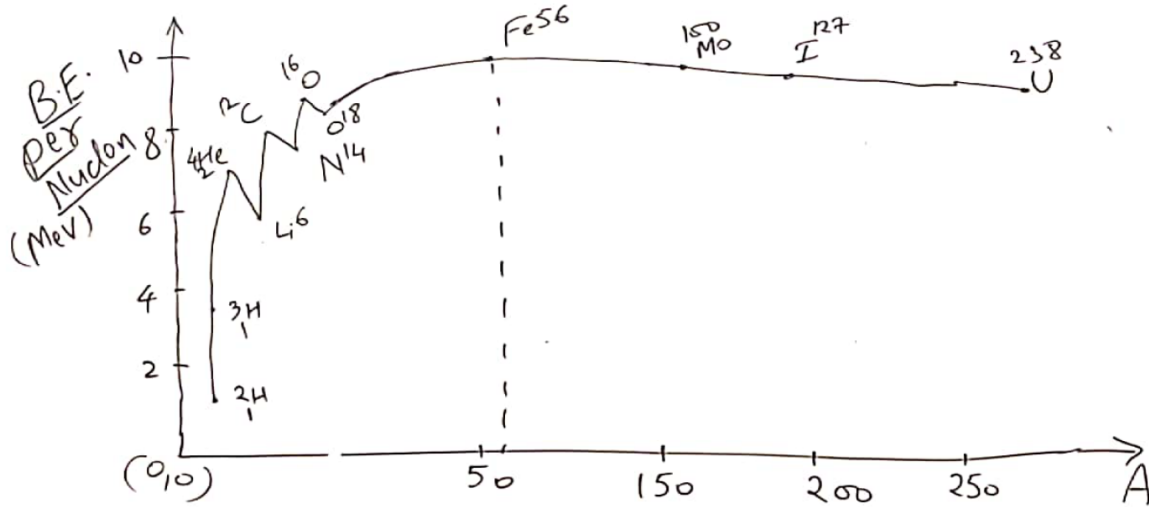
$$m({}_0^1\text{n}) = 1.008674$$

$$m({}_0^0\text{e}) = 0.00054864$$

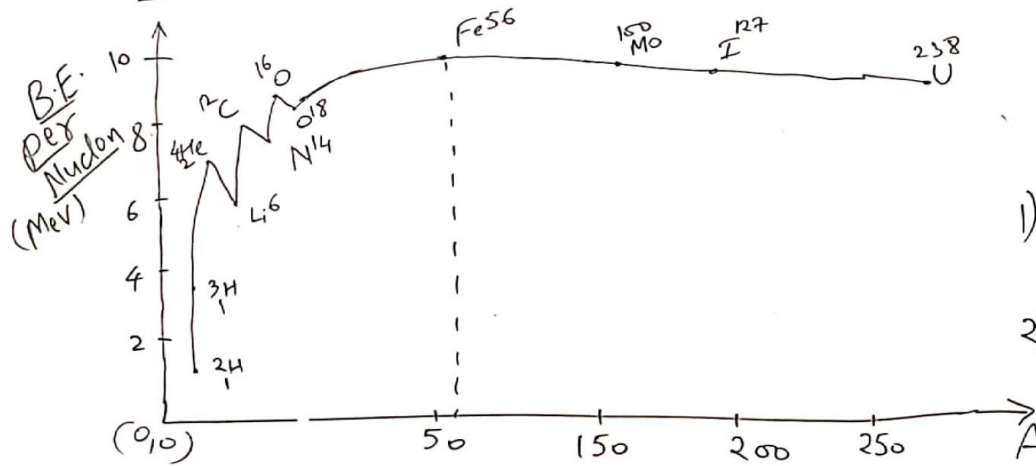
$$1u \equiv 931.5 \text{ MeV}/c^2$$

Criteria for stability

- binding energy
- \propto nucleon
- $(\Delta E/A)$
- if $(\Delta E/A) \uparrow$ stability \uparrow



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$$m({}_1^1\text{H}) = 1.00783u$$

$$m({}_1^0\text{n}) = 1.00867u$$

$$m({}_{-1}^0\text{e}) = 0.0005486u$$

$$1u \equiv 931.5 \text{ MeV}/c^2$$

1) $50 < A < 80$ → Nuclei are most stable. $(\Delta E/A) \sim 8 \text{ MeV}$

2) $A = 56 \rightarrow \text{Fe}_{26}^{56}$ → The most stable nucleus

3) $A > 80$, rate of decrease of $(B.E.)/A \rightarrow$ is lesser.

4) $A < 50$, rate of decrease of $(B.E.)/A \rightarrow$ is sharp.

5) For heavier nuclei → nucleus will split into lighter nuclei → Nuclear Fission.

$$\begin{array}{l}
 100 \\
 \text{Z} \rightarrow 55 \text{X} + 45 \text{Y} + \boxed{Q = 50 \text{ MeV}} \\
 \text{B.E. (MeV)} \quad 750 \quad 440 \quad 360 \rightarrow \text{total B.E.} = 800 \text{ MeV} \\
 (\text{B.E.}/A) \rightarrow 7.50/100 \quad 440/55 \quad 360/45 \\
 \quad \quad \quad 7.5 \quad = 8 \quad = 8
 \end{array}$$