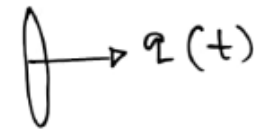


Current electricity

Defⁿ of Current: Rate of flow of charge.



I

$$I_{avg} = \frac{\Delta q}{\Delta t}$$

$$I_{ins} = \frac{dq}{dt}$$

Q1) Charge flow in Conductor
 $q = (2t^2 + 9t - 9)$ Coulomb

Sol) $q \rightarrow$ variable (or) Constant

$$i = \frac{dq}{dt}$$

(*) Slope of $q-t$ graph gives Current.

Current electricity

Q1) Charge in a conductor $q = (2t^2 + 4t - 5) \text{ C.}$
 find current in conductor at $t = 1 \text{ sec}$, 2 sec
 & 9 sec .

Sol) $i = \frac{dq}{dt} = \frac{d(2t^2 + 4t - 5)}{dt}$

$i = 2(2t^{2-1}) + 4 - 0$
 $i = 4t + 4 \rightarrow$ Current as function of time.

$t = 1 \text{ sec}$, $i_{t=1} = 4 \times 1 + 4 = 8 \text{ Amp.}$
 $t = 2$ $i_{t=2} = 4 \times 2 + 4 = 12 \text{ Amp.}$
 $t = 9$ $i_{t=9} = 4 \times 9 + 4 = 20 \text{ Amp.}$

$\frac{d2x^4}{dx} = 4x^{4-1} = 4x^3$
 Ex $\frac{d3x^4}{dx} = 3 \frac{d2x^4}{dx} = 3[4x^{4-1}] = 12x^3$

Q2) $Q = t^2 - 2t$. find current at $t = 1 \text{ sec}$ & 2 sec .
 & also find time when current is zero.

Solve) $Q = t^2 - 2t$

$i = \frac{dQ}{dt} = \frac{d(t^2 - 2t)}{dt}$

$i = 2t^{2-1} - 2(1t^{1-1}) = 2t - 2t^0 = 2t - 2$

$i = 2t - 2$
 $0 = 2t - 2$
 $2 = 2t$
 $t = 1 \text{ sec}$
 $t = 1$ $i_{t=1} = 2 \times 1 - 2 = 0$
 $t = 2$ $i_{t=2} = 2 \times 2 - 2 = 2 \text{ Amp}$

Charge flow in a Current electricity
Conductor

Q3) $Q = (t^3 - 6t^2 + 12) \text{ C}$. Find i at $t=0$ $t=1 \text{ sec}$ &

find time when $i=0$.

Solve:- $Q = (t^3 - 6t^2 + 12) \text{ C}$

$$i = \frac{dQ}{dt} = \frac{d}{dt} (t^3 - 6t^2 + 12)$$

$$i = 3t^{3-1} - 6(2t^{2-1}) + 0$$

$$i = 3t^2 - 12t$$

$$\underline{t=0}, i = 0 \text{ Amp}$$

$$t=1, i = 3 - 12 = -9 \text{ Amp}$$

$$i = 3t^2 - 12t$$

$$0 = \underline{3t} (\underline{t-4})$$

$$\underline{t=0}$$

$$t-4=0$$

$$t=4$$

Current electricity

Equ'n → Relation b/w i & q

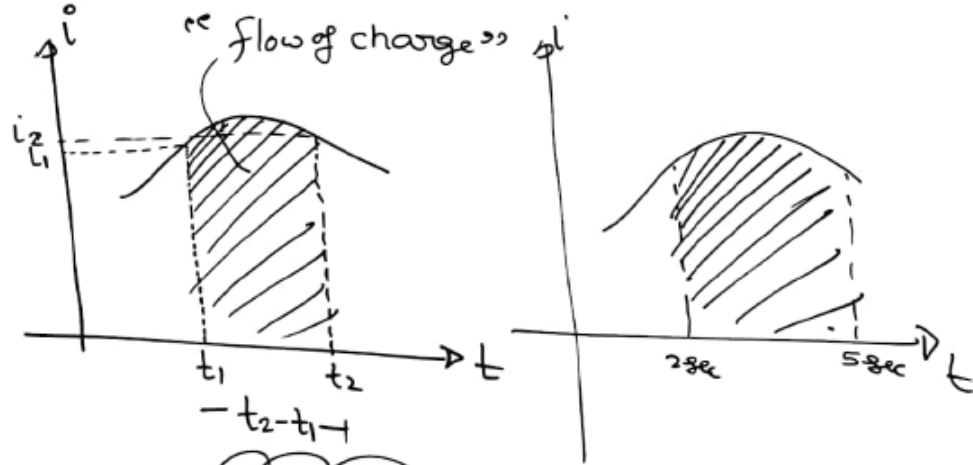
$$i = \frac{dq}{dt}$$

$$dq = \int_{t_1}^{t_2} i dt$$

$$q_{\text{flow}} = \int_{t_1}^{t_2} i dt$$



∴ area of $i-t$ graph
 area of current-time
 graph gives Total charge
 flow



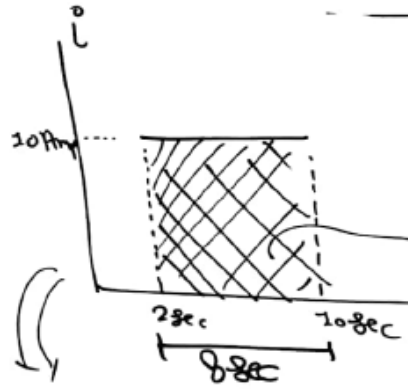
$i = \frac{dq}{dt}$

Slope of $(q-t)$ graph gives current

$q = \int i dt \Rightarrow$ area of $i-t$ graph
 gives total flow of charge

Current electricity

Q1



Find flow of charge in time blw 2 sec to 10 sec

area = 10×8
 $= 80 \text{ Coulomb}$
 $q_{\text{flow}} = 80 \text{ Coulomb}$

Matlab

$q = it$

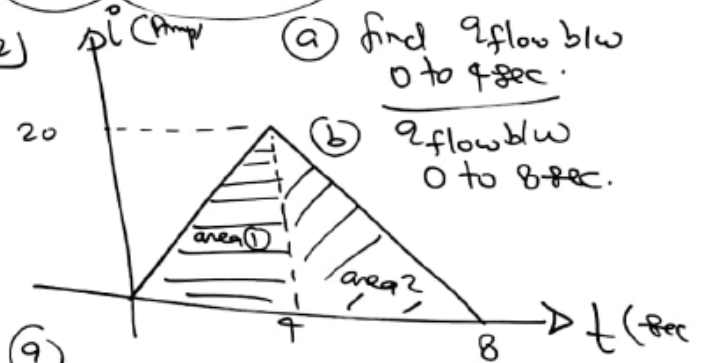
$10 \text{ Amp} = 10 \text{ C/sec}$

$q_{\text{flow}} = 10 \text{ C/sec} \times 8$
 $= 80 \text{ C}$

$q_{\text{flow}} = \int i dt$

Q2) i (Amp) (a) find q_{flow} blw 0 to 4 sec.

(b) q_{flow} blw 0 to 8 sec.

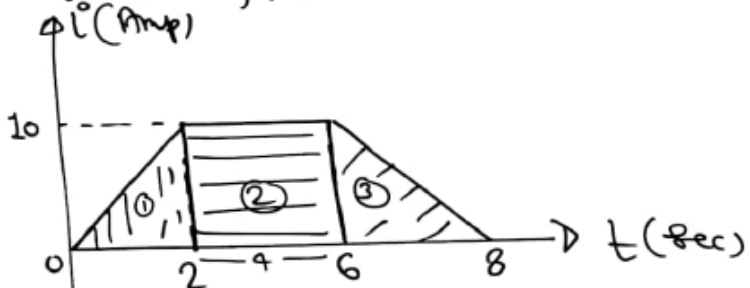


(a) $q_{\text{flow}(0-4)} = \text{Area of } (i-t) \text{ curve}$
 $= \frac{1}{2} \times 4 \times 20 = 40 \text{ C}$

(b) $q_{\text{flow}(0-8)} = \frac{1}{2} \times 8 \times 20 = 80 \text{ C}$

Current electricity

Q4) Find q_{flow} b/w $t=0$ to $t=8$ sec.



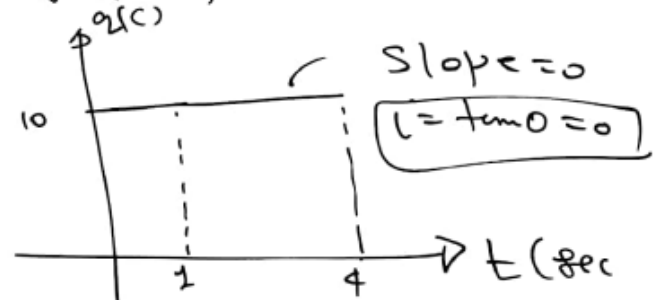
⇒ "Area of (It) - graph gives total q_{flow} "

$$\frac{1}{2} \times 2 \times 10 + 4 \times 10 + \frac{1}{2} \times 2 \times 10$$

$$10 + 40 + 10 = 60c$$

Q5)

Find q_{flow} b/w $t=2$ to $t=4$ sec



$$q_{flow} = 10 \text{ Coulombs}$$

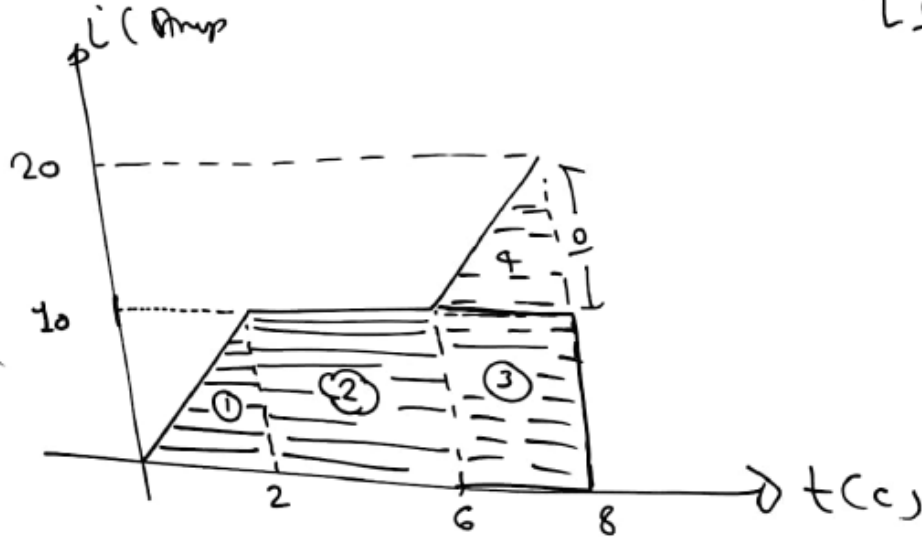
$i = 0$ [Slope of $i-t$ graph gives current]

→ $q_{t=1} = 10c$ ($\phi q = 0$)

$q_{t=4} = 10c$

Current electricity

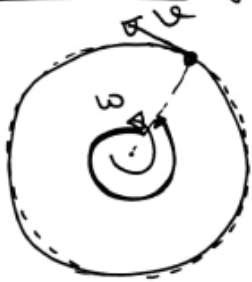
4) Find q_{flow} b/w $t=0$ to $t=8$ sec.



$$\begin{aligned}
 q_{flow} &= \textcircled{1} + \textcircled{2} + \textcircled{3} + \textcircled{4} \\
 &= \frac{1}{2} \times 2 \times 10 + 4 \times 10 + 2 \times 10 + \frac{1}{2} \times 2 \times 10 \\
 &= 10 + 40 + 20 + 10 \\
 &= \underline{\underline{80 \text{ Coulomb}}}
 \end{aligned}$$

Current electricity

\Rightarrow Angular velocity (ω) = $\frac{\text{Angular displacement}}{\text{time}}$



$\omega \rightarrow$ constant angular velocity

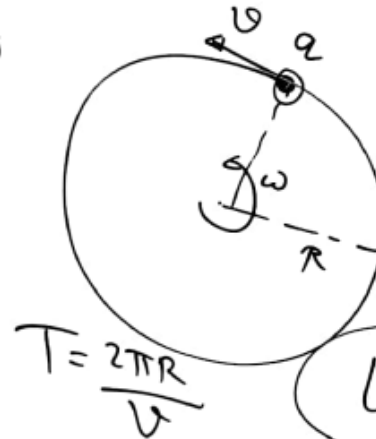
$\omega = \frac{2\pi}{T} = \frac{2\pi}{T} = 2\pi \left(\frac{1}{T} \right) = \underline{\underline{2\pi f}}$

$\omega = \frac{2\pi}{T} \Rightarrow T = \frac{2\pi}{\omega}$



\Rightarrow frequency (f) $\Rightarrow (f = \frac{1}{T})$

$T = \frac{2\pi R}{v}$ $v = \omega R$



$i_{av} = \frac{q}{T} = \frac{q}{T}$

$i_{av} = q \left(\frac{1}{T} \right) = \underline{\underline{qf}}$

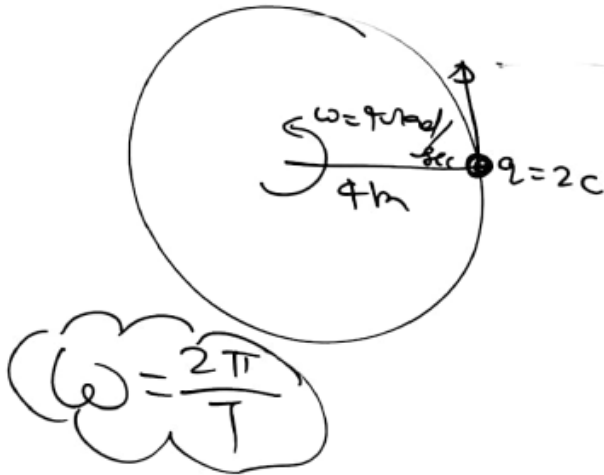
$i = \frac{q}{\frac{2\pi R}{v}} = \frac{qv}{2\pi R}$

$i = \frac{q}{\frac{2\pi}{\omega}} = \frac{q\omega}{2\pi}$

Current electricity

Q.1) A charge $q = 2\text{C}$ move in circular conducting path.
 radius 4m with angular velocity 9 rad/sec .
 find current in path.

$$\omega = \frac{2\pi}{T} \Rightarrow T = \frac{2\pi}{\omega}$$



$$i = \frac{q}{T}$$

$$i = \frac{q}{\frac{2\pi}{\omega}}$$

$$i = \frac{q\omega}{2\pi}$$

∴

$$i_{av} = \frac{q}{T} = \frac{q}{\frac{2\pi}{\omega}}$$

$$i_{av} = q \left(\frac{\omega}{2\pi} \right) = \frac{q\omega}{2\pi}$$

$$i = \frac{q}{\frac{2\pi R}{v}} = \frac{qv}{2\pi R}$$

$$i = \frac{q}{T} = \frac{q}{\frac{2\pi}{\omega}} = \frac{q\omega}{2\pi}$$