

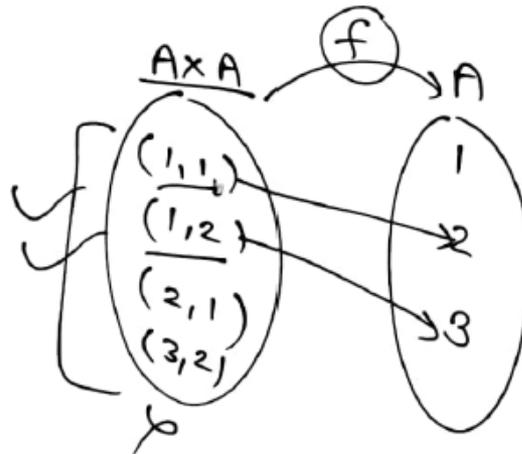
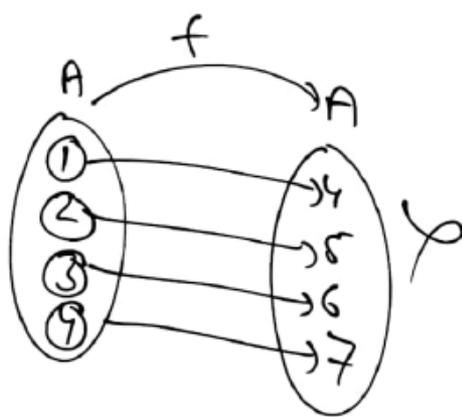
Relation & Function

Binary operation:- a Binary operation $*$ on a set A is a function
 as:- $*$: $A \times A \rightarrow A$ and we will denoted

$*$ as $(a, b) = a * b$

Ex:- $A = \{1, 2, 3\}$, $A = \{1, 2, 3\}$

$A \times A = \{(1,1)(1,2)(1,3)(2,1)(2,2)(2,3)(3,1)(3,2)(3,3)\}$



$a * b = a + b$
 $(1,1) = (1 * 1) = 1 + 1$
 $(1,2) = (1 * 2) = 1 + 2 = 3$

Relation & Function

Ex¹ Show that:- add., sub. & multi. are B.O. on \mathbb{R} .

but div. is not a B.O. on \mathbb{R} .

Sol^m:- $+$ is a B.O. i.e.

$+: \mathbb{R} \times \mathbb{R} \rightarrow \mathbb{R}$ given by $(a, b) = a + b$

\Rightarrow it is clear that $+$ is a function.

So it is a B.O. \checkmark

\Rightarrow Sub $\rightarrow (-) \rightarrow -$ is a B.O. i.e.:-

$-: \mathbb{R} \times \mathbb{R} \rightarrow \mathbb{R}$ given by:- $(a, b) = a - b$

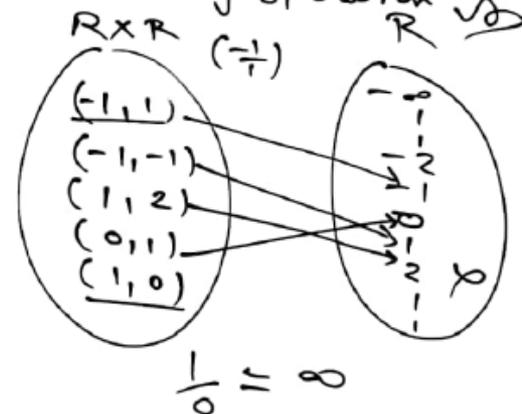
it is clear it is also B.O.

\Rightarrow $\times \rightarrow$ it is a B.O. i.e. $f_{\times}: \mathbb{R} \times \mathbb{R} \rightarrow \mathbb{R}$ given by:- $(a, b) = a \times b$

So it is clear that \times is also a B.O.

$\Rightarrow \div$ is a B.O. i.e. $f_{\div}: \mathbb{R} \times \mathbb{R} \rightarrow \mathbb{R}$

\because it is clear that for $(1, 0)$ there is no image in \mathbb{R} so: \div is not a function. Hence not a binary operation \checkmark



Relation & Function

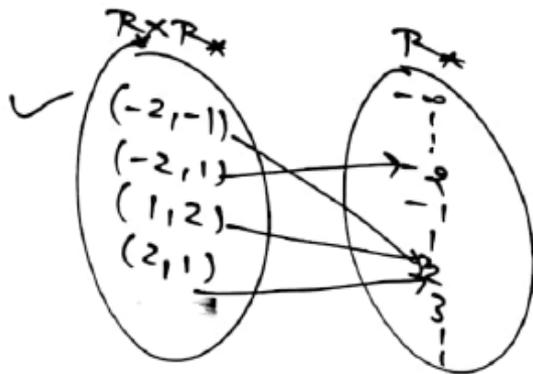
Ex:- Show that:- add., sub. & multi. are B.O. on \mathbb{R} .

but div. is not a B.O. on \mathbb{R} .

Show that:- division is a binary operation on set \mathbb{R}^* of nonzero Real no.

Solⁿ:- $\therefore \div$ is a B.O. \checkmark

function:- $\div : \mathbb{R}^* \times \mathbb{R}^* \rightarrow \mathbb{R}^*$ is define.



Here is lit clear that for all non-zero real no. there is a unique image of element $\mathbb{R}^* \times \mathbb{R}^*$ in \mathbb{R}^* . so it is a function & hence B.O. \checkmark

Relation & Function

Ex: Show that:-

Sub. & div. are not B.O. in \mathbb{N} .

Solⁿ: - $\therefore \boxed{- : \mathbb{N} \times \mathbb{N} \rightarrow \mathbb{N}}$ given by $\rightarrow (a, b) = a - b$

Here it is clear it is not a function.

So not a B.O. \checkmark

$\div : \mathbb{N} \times \mathbb{N} \rightarrow \mathbb{N} \rightarrow$ given by $(a, b) = a/b$

let $a = 5, b = 1 \Rightarrow \frac{a}{b} = \frac{5}{1} = \underline{5 \in \mathbb{N}}$

let $a = 5, b = 2 \Rightarrow \frac{a}{b} = \frac{5}{2} \notin \mathbb{N}$

Hence it is not a Bin and also not a B.O. \checkmark

$$\left\{ \begin{array}{l} a = 5, b = 1 \\ (a, b) = (5, 1) = 5 - 1 = 4 \\ \text{Now } a = 3, b = 5 \\ (3, 5) \in \mathbb{N} \\ (3, 5) = 3 - 5 = -2 \notin \mathbb{N} \end{array} \right.$$