

$$\begin{vmatrix} a+ib & c+id \\ -c+id & a-ib \end{vmatrix} = \frac{(a+ib)(a-ib)}{b^2} - \frac{(c+id)(-c+id)}{-b^2} \rightarrow [a^2 - (ib)^2] - [(id)^2 - c^2]$$

(a) $(a+b)^2$

(b) $(a+b+c+d)^2 \rightarrow a^2 + b^2 - [-d^2 - c^2]$

(c) $(a^2 + b^2 - c^2 - d^2)$

(d) $a^2 + b^2 + c^2 + d^2$ $a^2 + b^2 + d^2 + c^2$

$$\begin{vmatrix} \cos 15^\circ & \sin 15^\circ \\ \sin 75^\circ & \cos 75^\circ \end{vmatrix} =$$

$$\frac{\cos^A 15^\circ \cos^B 75^\circ - \sin^A 15^\circ \sin^B 75^\circ}{}$$

(a) 0

(b) 5

(c) 3

(d) 7

$$\cos(15+75)$$

$$\cos(90) = 0$$

$$\frac{\cos A \cos B - \sin A \sin B}{\cos(A+B)}$$

Consider the system of linear equations;

$$\begin{aligned} x_1 + 2x_2 + x_3 &= 3 \\ 2x_1 + 3x_2 + x_3 &= 3 \\ 3x_1 + 5x_2 + 2x_3 &= 1 \end{aligned}$$

inverse \rightarrow unique
 unique

The system has

- (a) exactly 3 solutions
- (b) a unique solution
- (c) no solution
- (d) infinite number of solutions

$$A = \begin{bmatrix} 1 & 2 & 1 \\ 2 & 3 & 1 \\ 3 & 5 & 2 \end{bmatrix}$$

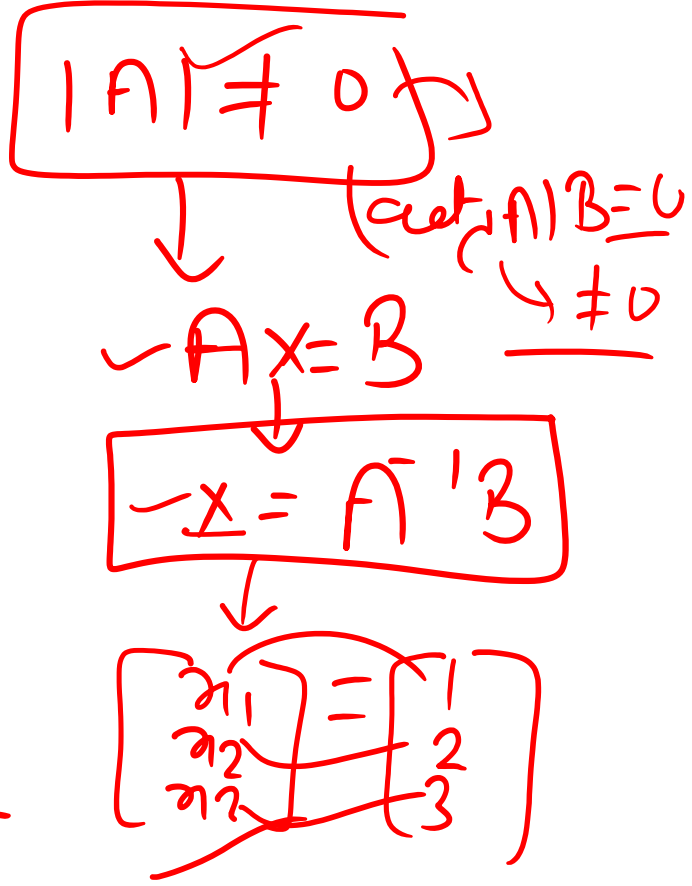
$A \rightarrow$ singular
 $A^{-1} \rightarrow$ exist

$x_1 \rightarrow 6$
 $x_2 \rightarrow 3$
 $x_3 \rightarrow 3$

$$|A| = \begin{vmatrix} 1 & 2 & 1 \\ 2 & 3 & 1 \\ 3 & 5 & 2 \end{vmatrix}$$

$$|A| = 1(6-5) - 2(4-3) + 1(10-9)$$

$$= 1 - 2 + 1 = 0 \quad \checkmark$$



For any 2×2 matrix A, if $A(\text{adj. } A) =$

$\begin{bmatrix} 10 & 0 \\ 0 & 10 \end{bmatrix}$, then $|A|$ is equal to :

(a) 0

(b) 10

(c) 20

(d) 100

$$|A| = ?$$

$$A \cdot A^{-1} |A| = 10 \cdot I$$

$$\Rightarrow \cancel{A} \cdot |A| = 10 \cdot \cancel{I}$$

$$\Rightarrow |A| = 10$$

$$\Rightarrow A \cdot (\text{adj } A) = \begin{bmatrix} 10 & 0 \\ 0 & 10 \end{bmatrix} = 10 \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$$

$$\Rightarrow [A(\text{adj } A)] = 10 \cdot I \quad \text{--- (1)}$$

$$\Rightarrow \therefore A^{-1} = \frac{1}{|A|} (\text{adj } A)$$

$$\Rightarrow \text{adj } A = A^{-1} \cdot |A| \quad \text{--- (2)}$$

If matrix $A = \begin{bmatrix} 3 & -2 & 4 \\ 1 & 2 & -1 \\ 0 & 1 & 1 \end{bmatrix}$ and $A^{-1} = \frac{1}{k}$

(adj A), then k is :

(a) 7

(c) 15

$$A^{-1} = \frac{1}{|A|} \cdot \text{adj}(A)$$

(b) -7

(d) -11

Soln:

give ✓

$$A^{-1} = \frac{1}{k} (\text{adj } A)$$

So: $|A| = k$

$$|A| = \begin{vmatrix} 3 & -2 & 4 \\ 1 & 2 & -1 \\ 0 & 1 & 1 \end{vmatrix} = -1(-3-4) + 1(6+2) = 7+8$$

If I_3 is the identity matrix of order 3, then

I_3^{-1} is

- (a) 0
- (b) $3I_3$
- (c) I_3
- (d) Does not exist

~~$\begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} \rightarrow A^{-1} = \frac{1}{|A|} \text{adj}(A)$~~

$A^{-1} = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} = I$

$I_2 = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} \rightarrow I_2$

$I_3 = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$

inverse \rightarrow same $\rightarrow I_3$

$I_3 = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$

$I_3 \rightarrow \text{inverse} \rightarrow I_3$

$I = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} = I = \frac{1}{|I|} \text{adj}(I) = \frac{1}{\begin{vmatrix} 1 & 0 \\ 0 & 1 \end{vmatrix}} \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} = I$

$\text{adj}(I) = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} = I$

If rows and columns of the determinant are interchanged, then its value

- (a) remains unchanged
- (b) becomes change
- (c) is doubled
- (d) is zero

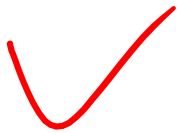
The diagram illustrates the interchange of rows and columns in a 3x3 determinant. The original matrix is shown as $\begin{vmatrix} 1 & 2 & 3 \\ 5 & 6 & 7 \\ 1 & 5 & 9 \end{vmatrix}$. A horizontal arrow above the matrix indicates the columns are swapped, and a vertical arrow to the right indicates the rows are swapped. This leads to the matrix $\begin{vmatrix} 1 & 5 & 9 \\ 2 & 6 & 7 \\ 3 & 5 & 7 \end{vmatrix} = \text{Same}$. A curved arrow on the left points from the original matrix to the swapped matrix.

If $[1 \times 1] \begin{bmatrix} 1 & 3 & 2 \\ 0 & 5 & 1 \\ 0 & 3 & 2 \end{bmatrix} \begin{bmatrix} x \\ x \\ -2 \end{bmatrix} = 0$, then x is $\frac{(1+id)(-(-+id))}{b \quad a \quad -b \quad a}$

(a) $-\frac{1}{2} \rightarrow \left[a^2 - (ib)^2 \right] - \left[(id)^2 - \left(\frac{1}{2}\right)^2 \right]$

(c) $1 \rightarrow a^2 + b^2 - \left[-d^2 - c^2 \right]$

$a^2 + b^2 + d^2 + c^2$



A square matrix $A = [a_{ij}]_{n \times n}$ is called a diagonal matrix if $a_{ij} = 0$ for

(a) $i=j$

(c) $i > j$

(b) $i < j$

(d) $i \neq j$

$\cos 15^\circ \cos 75^\circ - \sin 15^\circ \sin 75^\circ$

$\cos(15^\circ + 75^\circ)$

$\cos(90^\circ) = 0$

$\boxed{\cos A \cos B - \sin A \sin B}$
 $\underline{\cos(A+B)}$

If $P = \begin{bmatrix} i & 0 \\ 0 & -i \\ -i & i \end{bmatrix}$ and $Q = \begin{bmatrix} i & i \\ 0 & 0 \\ i & -i \end{bmatrix}$

then PQ is equal to

(a) $\begin{bmatrix} -2 & 2 \\ 1 & -1 \\ 1 & -1 \end{bmatrix}$ $A = \begin{bmatrix} 1 & 2 & 1 \\ 2 & 3 & 1 \\ 3 & 5 & 2 \end{bmatrix} \begin{bmatrix} 2 \\ -1 \\ -1 \end{bmatrix}$

(c) $\begin{bmatrix} 2 & -2 \\ -1 & 1 \end{bmatrix}$ $A = \begin{bmatrix} 1 & 2 & 0 \\ 2 & 3 & 0 \\ 3 & 5 & 2 \end{bmatrix} \begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix}$

$|A| \neq 0$

$AX = B$

$X = A^{-1}B$

$\begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix} = \begin{bmatrix} 1 \\ 2 \\ 3 \end{bmatrix}$

$|A| = \begin{vmatrix} 1 & 2 & 0 \\ 2 & 3 & 0 \\ 3 & 5 & 2 \end{vmatrix}$
 $|A| = 1(6-5) - 2(4-3) + 1(10-9)$
 $= 1 - 2 + 1 = 0 \checkmark A$

$A \rightarrow$ singular
 A^{-1} exist
 $\begin{matrix} x_1 = 1 \\ x_2 = 2 \\ x_3 = 3 \end{matrix}$

If a matrix A is both symmetric and skew-symmetric, then

- (a) A is a diagonal matrix
- (b) A is zero matrix
- (c) A is a scalar matrix
- (d) A is square matrix

$|A| = 9$ $A \cdot A^{-1} = 10 \cdot I$

$\Rightarrow \cancel{9} \cdot |A| = 10 \cdot \cancel{9}$

$\Rightarrow |A| = 10$

$\Rightarrow A \cdot (\text{adj } A) = \begin{bmatrix} 10 & 0 \\ 0 & 10 \end{bmatrix} = 10 \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$

$\Rightarrow [A(\text{adj } A)] = 10 \cdot I \quad \text{--- (1)}$

$\Rightarrow \therefore [A^{-1} = \frac{1}{|A|} \text{adj}(A)]$

$\Rightarrow \underline{\text{adj}(A)} = \underline{A^{-1} \cdot |A|} \quad \text{--- (2)}$

If A is a square matrix such that $A^2 = A$,

then $(I + A)^3 - 7A$ is equal to

- (a) A (b) $I - A$
 (c) I (d) $3A$

$A^{-1} = \frac{1}{|A|} \cdot \text{adj } A$

Sol: $A^{-1} = \frac{1}{K} (\text{adj } A)$ So: $|A| = K$

$|A| = \begin{vmatrix} 3 & -2 & 4 \\ 1 & 2 & -1 \\ 0 & 1 & 1 \end{vmatrix} = -1(3-4) + 1(6+2) = 7+8$

The matrix $\begin{bmatrix} 2 & 5 & -7 \\ 0 & 3 & 1 \\ 0 & 0 & 9 \end{bmatrix}$ is:

- (a) symmetric
- (b) diagonal
- (c) upper triangular
- (d) skew symmetric

$$I_3 = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

$I_3 \rightarrow \text{inverse} \rightarrow I_3 = \text{adj}(I) = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$

$$I_2 = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} \rightarrow I_2$$

$$I_3 = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

inverse \rightarrow same $\rightarrow I_3$

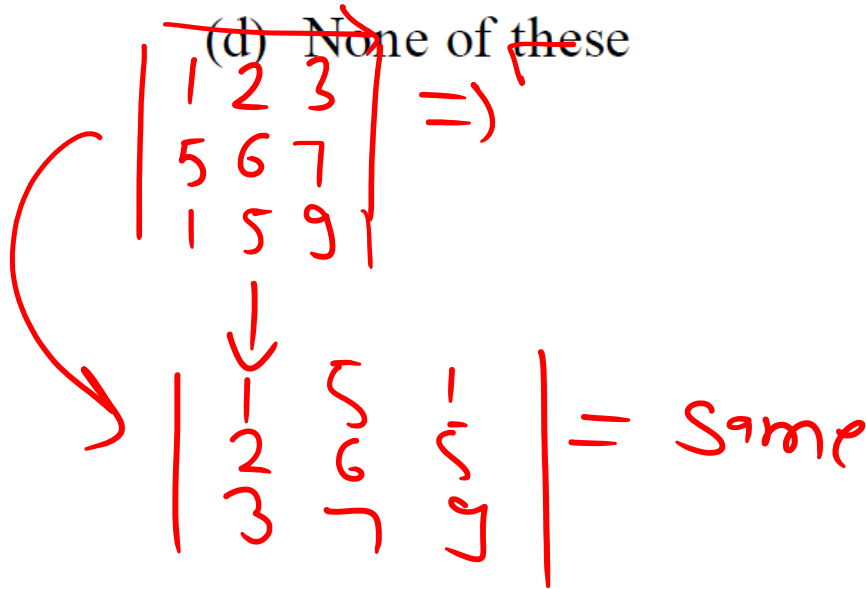
$$I = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} = |I| = \begin{vmatrix} 1 & 0 \\ 0 & 1 \end{vmatrix} = 1$$

$A^{-1} = \frac{1}{|A|} \cdot \text{adj}(A)$

If matrix $A = [a_{ij}]_{2 \times 2}$, where $a_{ij} =$

$\begin{cases} 1 & \text{if } i \neq j \\ 0 & \text{if } i = j \end{cases}$, then A^2 is equal to

- (a) I
- (b) A
- (c) O
- (d) None of these



Let $A = \{1, 2, 3, 4\}$, $B = \{1, 5, 9, 11, 15, 16\}$
 and $f = \{(1, 5), (2, 9), (3, 1), (4, 5), (2, 11)\}$.

Then,

- (a) f is a relation from A to B
- (b) f is a function from A to B
- (c) Both (a) and (b)
- (d) None of these

$$\frac{(a+ib)(a-ib) - (c+id)(c-id)}{b^2 - a^2}$$

$$\left[a^2 - (ib)^2 \right] \left[(id)^2 - (c)^2 \right]$$

$$\rightarrow a^2 + b^2 - [-d^2 - c^2]$$

$$a^2 + b^2 + d^2 + c^2$$



Let $n(A) = m$, and $n(B) = n$. Then the total number of non-empty relations that can be defined from A to B is

(a) m^n

(c) $mn - 1$

(b) $n^m - 1$

(d) $2^{mn} - 1$

$\cos 15^\circ \cos 75^\circ - \sin 15^\circ \sin 75^\circ$

$\cos(15^\circ + 75^\circ)$

$\cos(90^\circ) = 0$

$\cos A \cos B - \sin A \sin B = \cos(A + B)$

The relation R defined on the set $A = \{1, 2, 3, 4, 5\}$ by $R = \{(x, y) : |x^2 - y^2| < 16\}$ is given by \rightarrow unique

- (a) $\{(1, 1), (2, 1), (3, 1), (4, 1), (2, 3)\}$
- (b) $\{(2, 2), (3, 2), (4, 2), (2, 4)\}$
- (c) $\{(3, 3), (4, 3), (5, 4), (3, 4)\}$
- (d) None of these

$$A = \begin{bmatrix} 1 & 2 & 1 \\ 2 & 3 & 1 \\ 3 & 5 & 2 \end{bmatrix}$$

$A \rightarrow$ singular \rightarrow A^{-1} exist

$$\begin{matrix} x_1 = 5 \\ x_2 = 3 \\ x_3 = 3 \end{matrix}$$

$$|A| = \begin{vmatrix} 1 & 2 & 1 \\ 2 & 3 & 1 \\ 3 & 5 & 2 \end{vmatrix}$$

$$|A| = 1(6-5) - 2(4-3) + 1(10-9) = 1 - 2 + 1 = 0 \checkmark$$

$|A| \neq 0$

\downarrow (but $|A|B = 0 \neq 0$)

$\checkmark Ax = B$

\downarrow

$\checkmark x = A^{-1}B$

\downarrow

$\begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix} = \begin{bmatrix} 1 \\ 2 \\ 3 \end{bmatrix}$

If $A = \{8, 9, 10\}$ and $B = \{1, 2, 3, 4, 5\}$,

then the number of elements in $A \times A \times B$ is $|A| = ?$

are

\Rightarrow (a) $A \cdot (\text{card } A) = \begin{bmatrix} 0 & 0 \\ 0 & 10 \end{bmatrix} = 10 \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$
 \Rightarrow (a) $A \cdot (\text{card } A) = 10 \cdot I = 10$ (1)
 \Rightarrow (c) $45 \left[A^{-1} = \frac{1}{|A|} (\text{adj } A) \right]$
 \Rightarrow (c) $\text{card } (A) = \frac{A \cdot |A|}{|A|} = 2$ (2)

\Rightarrow $|A \times A \times B| = |A| \cdot |A| \cdot |B| = 10 \cdot 10 \cdot 5 = 500$
 \Rightarrow $|A| = 10$

(b) 30

(d) 75

If $n(X) = 5$ and $n(Y) = 7$, then the number of relations on $X \times Y$ is 2^{5m} . The value of 'm' is

- (a) 5 (b) 7
(c) 6 (d) 8

$A^{-1} = \frac{1}{|A|} \cdot \text{adj } A$

Sol: $A^{-1} = \frac{1}{K} (\text{adj } A)$ So: $|A| = K$

$|A| = \begin{vmatrix} 3 & -2 & 4 \\ 1 & 2 & -1 \\ 0 & 1 & 1 \end{vmatrix} = -1(3-4) + 1(6+2) = 7+8$

